## Section 5: RL

## 1 Learning in Gridworld

Consider the example gridworld that we looked at in lecture. We would like to use TD learning and q-learning to find the values of these states.


Suppose that we have the following observed transitions:
(B, East, C, 2), (C, South, E, 4), (C, East, A, 6), (B, East, C, 2)
The initial value of each state is 0 . Assume that $\gamma=1$ and $\alpha=0.5$.

1. What are the learned values from TD learning after all four observations?
2. What are the learned Q-values from Q-learning after all four observations?

## Q2. Pacman with Feature-Based Q-Learning

We would like to use a Q-learning agent for Pacman, but the size of the state space for a large grid is too massive to hold in memory. To solve this, we will switch to feature-based representation of Pacman's state.

1. We will have two features, $F_{g}$ and $F_{p}$, defined as follows:

$$
\begin{aligned}
& F_{g}(s, a)=A(s)+B(s, a)+C(s, a) \\
& F_{p}(s, a)=D(s)+2 E(s, a)
\end{aligned}
$$

where

$$
\begin{aligned}
A(s) & =\text { number of ghosts within } 1 \text { step of state } s \\
B(s, a) & =\text { number of ghosts Pacman touches after taking action } a \text { from state } s \\
C(s, a) & =\text { number of ghosts within } 1 \text { step of the state Pacman ends up in after taking action } a \\
D(s) & =\text { number of food pellets within } 1 \text { step of state } s \\
E(s, a) & =\text { number of food pellets eaten after taking action } a \text { from state } s
\end{aligned}
$$

For this pacman board, the ghosts will always be stationary, and the action space is $\{$ left, right, up, down, stay $\}$.

calculate the features for the actions $\in\{$ left, right, up, stay $\}$
2. After a few episodes of Q -learning, the weights are $w_{g}=-10$ and $w_{p}=100$. Calculate the Q value for each action $\in\{l e f t$, right, up, stay $\}$ from the current state shown in the figure.
3. We observe a transition that starts from the state above, $s$, takes action $u p$, ends in state $s^{\prime}$ (the state with the food pellet above) and receives a reward $R\left(s, a, s^{\prime}\right)=250$. The available actions from state $s^{\prime}$ are down and stay. Assuming a discount of $\gamma=0.5$, calculate the new estimate of the Q value for $s$ based on this episode.
4. With this new estimate and a learning rate $(\alpha)$ of 0.5 , update the weights for each feature.

## Q3. MDPs and RL



Consider the above gridworld. An agent is currently on grid cell $S$, and would like to collect the rewards that lie on both sides of it. If the agent is on a numbered square, its only available action is to Exit, and when it exits it gets reward equal to the number on the square. On any other (non-numbered) square, its available actions are to move East and West. Note that North and South are never available actions.

If the agent is in a square with an adjacent square downward, it does not always move successfully: when the agent is in one of these squares and takes a move action, it will only succeed with probability $p$. With probability $1-p$, the move action will fail and the agent will instead move downwards. If the agent is not in a square with an adjacent space below, it will always move successfully.

For parts (a) and (b), we are using discount factor $\gamma \in[0,1]$.
(a) Consider the policy $\pi_{\text {East }}$, which is to always move East (right) when possible, and to Exit when that is the only available action. For each non-numbered state $x$ in the diagram below, fill in $V^{\pi}$ East $(x)$ in terms of $\gamma$ and $p$.

(b) Consider the policy $\pi_{\text {West }}$, which is to always move West (left) when possible, and to Exit when that is the only available action. For each non-numbered state $x$ in the diagram below, fill in $V^{\pi_{\text {West }}(x)}$ in terms of $\gamma$ and $p$.

(c) For what range of values of $p$ in terms of $\gamma$ is it optimal for the agent to go West (left) from the start state $(S)$ ?

## Range:

(d) For what range of values of $p$ in terms of $\gamma$ is $\pi_{\text {West }}$ the optimal policy?

Range: $\qquad$
(e) For what range of values of $p$ in terms of $\gamma$ is $\pi_{\text {East }}$ the optimal policy?

Range: $\qquad$

